

# PROPAGATION FORMULAS

## 1.1 DBW FROM VOLTAGE OR POWER

$$\text{Power in dBW} = 10 \text{ Log} \left( \frac{(\text{Voltage in microvolts} \times 10^{-6})^2}{50 \text{ ohms}} \right)$$

$$\text{Power in dBW} = 10 \text{ Log} \left( \frac{(\text{Voltage in volts})^2}{50 \text{ ohms}} \right)$$

$$\text{Power in dBW} = 10 \text{ Log} (\text{Power in watts})$$

Note: dBW = dBm - 30 dB

## 1.2 FREQUENCY TO WAVELENGTH

$$\text{Wavelength in Meters} = \frac{300}{f_{\text{MHz}}}$$

$$\text{Wavelength in Feet} = \frac{984}{f \text{ MHz}}$$

## 1.3 FREE SPACE LOSS

$$\text{Half Wave Dipole (distance in miles)} \quad \text{dB} = 32.28 + 20 \text{ LOG } f_{\text{MHz}} + 20 \text{ LOG } D_{\text{mi}}$$

$$\text{Isotropic radiator (distance in miles)} \quad \text{dB} = 36.58 + 20 \text{ LOG } f_{\text{MHz}} + 20 \text{ LOG } D_{\text{mi}}$$

$$\text{Half Wave Dipoles (distance in Kilometers)} \quad \text{dB} = 88.15 + 20 \text{ LOG } f_{\text{GHz}} + 20 \text{ LOG } D_{\text{km}}$$

Isotropic radiator (distance in kilometers)  $dB = 92.45 + 20 \text{ LOG } f_{\text{GHz}} + 20 \text{ LOG } D_{\text{km}}$

## 1.4 EARTH CURVATURE

	<u>d in miles, h in feet</u>	<u>d in kilometers, h in meters</u>
General	$h = \frac{d_1 d_2}{1.5K}$	$h = \frac{d_1 d_2}{12.75K}$
$K = \infty$	$h = 0$	$h = 0$
$K = 4/3$	$h = \frac{d_1 d_2}{2}$	$h = \frac{d_1 d_2}{17}$
$K = 2/3$	$h = d_1 d_2$	$h = \frac{d_1 d_2}{8.5}$
$K = 1$	$h = 0.67 d_1 d_2$	$h = \frac{d_1 d_2}{12.75}$

Where  $h$  = the change in vertical distance from a horizontal reference line, in feet/meters

$d_1$  = the distance from a point to one end of the path in miles/kilometers

$d_2$  = the distance from the same point to the other end of the path, in miles/kilometers

$K$  = the equivalent earth radius factor

## 1.5 FRESNEL ZONE

Feet  $F_1 = 72.1 \sqrt{\frac{d_1 d_2}{(f_{\text{GHz}})D}}$   $d_1, d_2, D$  in miles

Meters  $F_1 = 17.3 \sqrt{\frac{d_1 d_2}{(f_{\text{GHz}})D}}$   $d_1, d_2, D$  in kilometers

Where:  $F_1$  = first Fresnel zone radius in feet/meters

$d_1$  = distance from one end of path to reflection point

$d_2 = D - d_1$

$D$  = Total length of path

$f$  = frequency in GHz

Note: These formulas provide the distance to the first Fresnel Zone. If "0.6" Fresnel is required then multiply by "0.6".

## **1.6 DISTANCE TO RADIO HORIZON**

$$\text{General} \quad D = \sqrt{\frac{3Kh}{2}}$$

$$K=1 \quad D = \sqrt{1.5h}$$

$$K = 4/3 \quad D = \sqrt{2h}$$

Where:  $D$  = distance to the radio horizon in miles  
 $K$  = the equivalent earth radius factor  
 $h$  = height in feet

## **1.7 FIELD STRENGTH TO SENSITIVITY**

$$uV = \frac{39.5 * (uV / m)}{f_{\text{MHz}}}$$

$$F_{\text{dBuV / m}} = 20 \text{ Log } E_{(uV / m)}$$

$$F_{\text{dBuV / m}} = 105 + 10 \text{ Log } P_{(\text{Watts})} + 20 \text{ Log}(f_{\text{MHz}})$$

$$F_{\text{dBuV / m}} = 75 + 10 \text{ Log } P_{(\text{milliWatts})} + 20 \text{ Log}(f_{\text{MHz}})$$

$$\frac{\text{dBW}}{\text{m}^2} = \text{dBm} - 70.65 + 20 \text{ Log}(f_{\text{MHz}})$$

Where  $F$  = field strength in dB microvolts per meter

$P$  = power

$f$  = frequency

Note: For 50 ohms, referenced to a dipole.

## **1.8 DOPPLER SHIFT**

$$v(\text{km / h}) = 1079 * \frac{\Delta f_{\text{Hz}}}{f_{\text{MHz}}}$$

$$\Delta f_{\text{Hz}} = 0.009266 * v(\text{km / h}) * f_{\text{MHz}}$$

$$v(\text{m / h}) = 670.6 * \frac{\Delta f_{\text{Hz}}}{f_{\text{MHz}}}$$

$$\Delta f_{\text{Hz}} = 0.00149 * v(\text{m / h}) * f_{\text{MHz}}$$

Where  $v$  = velocity

## **1.9 NEAR FIELD / FAR FIELD BOUNDARY**

$$\text{Far Field Starts at: } \frac{983}{f_{\text{MHz}}} * 10^{\frac{G_{\text{dBd}}}{10}} \text{ (meters)}$$

$$\text{Far Field Starts at: } \frac{3226}{f_{\text{MHz}}} * 10^{\frac{G_{\text{dBd}}}{10}} \text{ (feet)}$$

Where:  $G_{\text{dBd}}$  = Gain referenced to a dipole

## **1.10 NOISE POWER**

$$P_{\text{N(Watts)}} = kTB$$

Where:  $k$  = Boltzman's constant =  $1.38 * 10^{-23} \frac{J}{K}$

$B$  = Bandwidth in Hz

$T$  = 290 Kelvin

Noise power in dBm is  $P_{\text{N}} = -143.9 + 10\text{Log}(B_{\text{kHz}})$

**FORMULA REFERENCES:**

1-1 Engineering Considerations for Microwave Communications Systems, Fourth Edition, GTE Lenkurt Inc., 1975

**MICROVOLT TO dBW and dBm**

<b>Microvolt</b>	<b>dBW</b>	<b>dBm</b>	<b>Microvolt</b>	<b>dBW</b>	<b>dBm</b>	<b>Microvolt</b>	<b>dBW</b>	<b>dBm</b>
<b>0.10</b>	-156.99	-126.99	<b>0.58</b>	-141.72	-111.72	<b>1.06</b>	-136.48	-106.48
<b>0.11</b>	-156.16	-126.16	<b>0.59</b>	-141.57	-111.57	<b>1.07</b>	-136.40	-106.40
<b>0.12</b>	-155.41	-125.41	<b>0.60</b>	-141.43	-111.43	<b>1.08</b>	-136.32	-106.32
<b>0.13</b>	-154.71	-124.71	<b>0.61</b>	-141.28	-111.28	<b>1.09</b>	-136.24	-106.24
<b>0.14</b>	-154.07	-124.07	<b>0.62</b>	-141.14	-111.14	<b>1.10</b>	-136.16	-106.16
<b>0.15</b>	-153.47	-123.47	<b>0.63</b>	-141.00	-111.00	<b>1.11</b>	-136.08	-106.08
<b>0.16</b>	-152.91	-122.91	<b>0.64</b>	-140.87	-110.87	<b>1.12</b>	-136.01	-106.01
<b>0.17</b>	-152.38	-122.38	<b>0.65</b>	-140.73	-110.73	<b>1.13</b>	-135.93	-105.93
<b>0.18</b>	-151.88	-121.88	<b>0.66</b>	-140.60	-110.60	<b>1.14</b>	-135.85	-105.85
<b>0.19</b>	-151.41	-121.41	<b>0.67</b>	-140.47	-110.47	<b>1.15</b>	-135.78	-105.78
<b>0.20</b>	-150.97	-120.97	<b>0.68</b>	-140.34	-110.34	<b>1.16</b>	-135.70	-105.70
<b>0.21</b>	-150.55	-120.55	<b>0.69</b>	-140.21	-110.21	<b>1.17</b>	-135.63	-105.63
<b>0.22</b>	-150.14	-120.14	<b>0.70</b>	-140.09	-110.09	<b>1.18</b>	-135.55	-105.55
<b>0.23</b>	-149.76	-119.76	<b>0.71</b>	-139.96	-109.96	<b>1.19</b>	-135.48	-105.48
<b>0.24</b>	-149.39	-119.39	<b>0.72</b>	-139.84	-109.84	<b>1.20</b>	-135.41	-105.41
<b>0.25</b>	-149.03	-119.03	<b>0.73</b>	-139.72	-109.72	<b>1.21</b>	-135.33	-105.33
<b>0.26</b>	-148.69	-118.69	<b>0.74</b>	-139.61	-109.61	<b>1.22</b>	-135.26	-105.26
<b>0.27</b>	-148.36	-118.36	<b>0.75</b>	-139.49	-109.49	<b>1.23</b>	-135.19	-105.19
<b>0.28</b>	-148.05	-118.05	<b>0.76</b>	-139.37	-109.37	<b>1.24</b>	-135.12	-105.12
<b>0.29</b>	-147.74	-117.74	<b>0.77</b>	-139.26	-109.26	<b>1.25</b>	-135.05	-105.05
<b>0.30</b>	-147.45	-117.45	<b>0.78</b>	-139.15	-109.15	<b>1.26</b>	-134.98	-104.98
<b>0.31</b>	-147.16	-117.16	<b>0.79</b>	-139.04	-109.04	<b>1.27</b>	-134.91	-104.91
<b>0.32</b>	-146.89	-116.89	<b>0.80</b>	-138.93	-108.93	<b>1.28</b>	-134.85	-104.85
<b>0.33</b>	-146.62	-116.62	<b>0.81</b>	-138.82	-108.82	<b>1.29</b>	-134.78	-104.78
<b>0.34</b>	-146.36	-116.36	<b>0.82</b>	-138.71	-108.71	<b>1.30</b>	-134.71	-104.71
<b>0.35</b>	<b>-146.11</b>	<b>-116.11</b>	<b>0.83</b>	-138.61	-108.61	<b>1.31</b>	-134.64	-104.64
<b>0.36</b>	-145.86	-115.86	<b>0.84</b>	-138.50	-108.50	<b>1.32</b>	-134.58	-104.58
<b>0.37</b>	-145.63	-115.63	<b>0.85</b>	-138.40	-108.40	<b>1.33</b>	-134.51	-104.51
<b>0.38</b>	-145.39	-115.39	<b>0.86</b>	-138.30	-108.30	<b>1.34</b>	-134.45	-104.45
<b>0.39</b>	-145.17	-115.17	<b>0.87</b>	-138.20	-108.20	<b>1.35</b>	-134.38	-104.38
<b>0.40</b>	-144.95	-114.95	<b>0.88</b>	-138.10	-108.10	<b>1.36</b>	-134.32	-104.32
<b>0.41</b>	-144.73	-114.73	<b>0.89</b>	-138.00	-108.00	<b>1.37</b>	-134.26	-104.26
<b>0.42</b>	-144.52	-114.52	<b>0.90</b>	-137.90	-107.90	<b>1.38</b>	-134.19	-104.19
<b>0.43</b>	-144.32	-114.32	<b>0.91</b>	-137.81	-107.81	<b>1.39</b>	-134.13	-104.13
<b>0.44</b>	-144.12	-114.12	<b>0.92</b>	-137.71	-107.71	<b>1.40</b>	-134.07	-104.07
<b>0.45</b>	-143.93	-113.93	<b>0.93</b>	-137.62	-107.62	<b>1.41</b>	-134.01	-104.01
<b>0.46</b>	-143.73	-113.73	<b>0.94</b>	-137.53	-107.53	<b>1.42</b>	-133.94	-103.94
<b>0.47</b>	-143.55	-113.55	<b>0.95</b>	-137.44	-107.44	<b>1.43</b>	-133.88	-103.88
<b>0.48</b>	-143.36	-113.36	<b>0.96</b>	-137.34	-107.34	<b>1.44</b>	-133.82	-103.82
<b>0.49</b>	-143.19	-113.19	<b>0.97</b>	-137.25	-107.25	<b>1.45</b>	-133.76	-103.76
<b>0.50</b>	<b>-143.01</b>	<b>-113.01</b>	<b>0.98</b>	-137.17	-107.17	<b>1.46</b>	-133.70	-103.70
<b>0.51</b>	-142.84	-112.84	<b>0.99</b>	-137.08	-107.08	<b>1.47</b>	-133.64	-103.64
<b>0.52</b>	-142.67	-112.67	<b>1.00</b>	-136.99	-106.99	<b>1.48</b>	-133.58	-103.58
<b>0.53</b>	-142.50	-112.50	<b>1.01</b>	-136.90	-106.90	<b>1.49</b>	-133.53	-103.53

<b>0.54</b>	-142.34	-112.34	<b>1.02</b>	-136.82	-106.82	<b>1.50</b>	-133.47	-103.47
<b>0.55</b>	-142.18	-112.18	<b>1.03</b>	-136.73	-106.73	<b>1.51</b>	-133.41	-103.41
<b>0.56</b>	-142.03	-112.03	<b>1.04</b>	-136.65	-106.65	<b>1.52</b>	-133.35	-103.35
<b>0.57</b>	-141.87	-111.87	<b>1.05</b>	-136.57	-106.57	<b>1.53</b>	-133.30	-103.30
<b>1.54</b>	-133.24	-103.24	<b>2.01</b>	-130.93	-100.93	<b>2.48</b>	-129.10	-99.10
<b>1.55</b>	-133.18	-103.18	<b>2.02</b>	-130.88	-100.88	<b>2.49</b>	-129.07	-99.07
<b>1.56</b>	-133.13	-103.13	<b>2.03</b>	-130.84	-100.84	<b>2.50</b>	-129.03	-99.03
<b>1.57</b>	-133.07	-103.07	<b>2.04</b>	-130.80	-100.80	<b>2.51</b>	-129.00	-99.00
<b>1.58</b>	-133.02	-103.02	<b>2.05</b>	-130.75	-100.75	<b>2.52</b>	-128.96	-98.96
<b>1.59</b>	-132.96	-102.96	<b>2.06</b>	-130.71	-100.71	<b>2.53</b>	-128.93	-98.93
<b>1.60</b>	-132.91	-102.91	<b>2.07</b>	-130.67	-100.67	<b>2.54</b>	-128.89	-98.89
<b>1.61</b>	-132.85	-102.85	<b>2.08</b>	-130.63	-100.63	<b>2.55</b>	-128.86	-98.86
<b>1.62</b>	-132.80	-102.80	<b>2.09</b>	-130.59	-100.59	<b>2.56</b>	-128.82	-98.82
<b>1.63</b>	-132.75	-102.75	<b>2.10</b>	-130.55	-100.55	<b>2.57</b>	-128.79	-98.79
<b>1.64</b>	-132.69	-102.69	<b>2.11</b>	-130.50	-100.50	<b>2.58</b>	-128.76	-98.76
<b>1.65</b>	-132.64	-102.64	<b>2.12</b>	-130.46	-100.46	<b>2.59</b>	-128.72	-98.72
<b>1.66</b>	-132.59	-102.59	<b>2.13</b>	-130.42	-100.42	<b>2.60</b>	-128.69	-98.69
<b>1.67</b>	-132.54	-102.54	<b>2.14</b>	-130.38	-100.38	<b>2.61</b>	-128.66	-98.66
<b>1.68</b>	-132.48	-102.48	<b>2.15</b>	-130.34	-100.34	<b>2.62</b>	-128.62	-98.62
<b>1.69</b>	-132.43	-102.43	<b>2.16</b>	-130.30	-100.30	<b>2.63</b>	-128.59	-98.59
<b>1.70</b>	-132.38	-102.38	<b>2.17</b>	-130.26	-100.26	<b>2.64</b>	-128.56	-98.56
<b>1.71</b>	-132.33	-102.33	<b>2.18</b>	-130.22	-100.22	<b>2.65</b>	-128.52	-98.52
<b>1.72</b>	-132.28	-102.28	<b>2.19</b>	-130.18	-100.18	<b>2.66</b>	-128.49	-98.49
<b>1.73</b>	-132.23	-102.23	<b>2.20</b>	-130.14	-100.14	<b>2.67</b>	-128.46	-98.46
<b>1.74</b>	-132.18	-102.18	<b>2.21</b>	-130.10	-100.10	<b>2.68</b>	-128.43	-98.43
<b>1.75</b>	-132.13	-102.13	<b>2.22</b>	-130.06	-100.06	<b>2.69</b>	-128.39	-98.39
<b>1.76</b>	-132.08	-102.08	<b>2.23</b>	-130.02	-100.02	<b>2.70</b>	-128.36	-98.36
<b>1.77</b>	-132.03	-102.03	<b>2.24</b>	-129.98	-99.98	<b>2.71</b>	-128.33	-98.33
<b>1.78</b>	-131.98	-101.98	<b>2.25</b>	-129.95	-99.95	<b>2.72</b>	-128.30	-98.30
<b>1.79</b>	-131.93	-101.93	<b>2.26</b>	-129.91	-99.91	<b>2.73</b>	-128.27	-98.27
<b>1.80</b>	-131.88	-101.88	<b>2.27</b>	-129.87	-99.87	<b>2.74</b>	-128.23	-98.23
<b>1.81</b>	-131.84	-101.84	<b>2.28</b>	-129.83	-99.83	<b>2.75</b>	-128.20	-98.20
<b>1.82</b>	-131.79	-101.79	<b>2.29</b>	-129.79	-99.79	<b>2.76</b>	-128.17	-98.17
<b>1.83</b>	-131.74	-101.74	<b>2.30</b>	-129.76	-99.76	<b>2.77</b>	-128.14	-98.14
<b>1.84</b>	-131.69	-101.69	<b>2.31</b>	-129.72	-99.72	<b>2.78</b>	-128.11	-98.11
<b>1.85</b>	-131.65	-101.65	<b>2.32</b>	-129.68	-99.68	<b>2.79</b>	-128.08	-98.08
<b>1.86</b>	-131.60	-101.60	<b>2.33</b>	-129.64	-99.64	<b>2.80</b>	-128.05	-98.05
<b>1.87</b>	-131.55	-101.55	<b>2.34</b>	-129.61	-99.61	<b>2.81</b>	-128.02	-98.02
<b>1.88</b>	-131.51	-101.51	<b>2.35</b>	-129.57	-99.57	<b>2.82</b>	-127.98	-97.98
<b>1.89</b>	-131.46	-101.46	<b>2.36</b>	-129.53	-99.53	<b>2.83</b>	-127.95	-97.95
<b>1.90</b>	-131.41	-101.41	<b>2.37</b>	-129.49	-99.49	<b>2.84</b>	-127.92	-97.92
<b>1.91</b>	-131.37	-101.37	<b>2.38</b>	-129.46	-99.46	<b>2.85</b>	-127.89	-97.89
<b>1.92</b>	-131.32	-101.32	<b>2.39</b>	-129.42	-99.42	<b>2.86</b>	-127.86	-97.86
<b>1.93</b>	-131.28	-101.28	<b>2.40</b>	-129.39	-99.39	<b>2.87</b>	-127.83	-97.83
<b>1.94</b>	-131.23	-101.23	<b>2.41</b>	-129.35	-99.35	<b>2.88</b>	-127.80	-97.80
<b>1.95</b>	-131.19	-101.19	<b>2.42</b>	-129.31	-99.31	<b>2.89</b>	-127.77	-97.77
<b>1.96</b>	-131.14	-101.14	<b>2.43</b>	-129.28	-99.28	<b>2.90</b>	-127.74	-97.74
<b>1.97</b>	-131.10	-101.10	<b>2.44</b>	-129.24	-99.24	<b>2.91</b>	-127.71	-97.71
<b>1.98</b>	-131.06	-101.06	<b>2.45</b>	-129.21	-99.21	<b>2.92</b>	-127.68	-97.68
<b>1.99</b>	-131.01	-101.01	<b>2.46</b>	-129.17	-99.17	<b>2.93</b>	-127.65	-97.65
<b>2.00</b>	-130.97	-100.97	<b>2.47</b>	-129.14	-99.14	<b>2.94</b>	-127.62	-97.62

